
hlmm Documentation

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CHAPTER 1

Introduction

`block_sparse` is a python library for performing computations with

CHAPTER 2

Tutorial

Documentation for ‘block_sparse’ module

Documentation for the `regnd` model class.

class `block_sparse.block_sparse` (*blocks*, *nonzero*, *submatrices*, *dtype*=<type ‘numpy.float32’>, *row_names*=None, *col_names*=None)

Define a block-sparse matrix

Parameters **blocks** : list

list of [row_block_boundaries,col_block_boundaries], where each of row_block_boundaries and col_block_boundaries is a 1D array of integers, beginning with 0, followed by the end boundaries of each block in increasing order

nonzero : array

boolean numpy array with number of rows equal to number of row blocks, and number of columns equal to number of col blocks. If entry [i,j] of nonzero is True, then the corresponding block is non-zero; if it is False, then the corresponding block is zero.

submatrices : list

list of submatrices for non-zero blocks in row-major order; e.g., block (1,1), (1,2), (2,1), (2,2),... Each submatrix can be an array, a *block_sparse* matrix, or a *symmetric_block_sparse* matrix.

dtype : numpy data type object

Set the default data type for the submatrices. Default `float32`

row_names : array

numpy array with names of the row-blocks. Default None

col_names : array

numpy array with names of the col-blocks. Default None

Returns **matrix** : *block_sparse*

block-sparse matrix

Methods

<code>add(A)</code>	Matrix addition of a matrix A to current matrix
<code>dot(A)</code>	Right multiply the current matrix with another <i>block_sparse</i> matrix, <i>symmetric_block_sparse</i> matrix, or array, A.
<code>frobenius(A)</code>	Compute the frobenius inner product between the current matrix and matrix A
<code>get_submatrix(block)</code>	Retrieve a particular block of the matrix
<code>get_type(block)</code>	Retrieve the type of a particular block of the matrix
<code>norm()</code>	Compute the frobenius norm of the current matrix
<code>qform(y[, z])</code>	Computes quadratic form defined by current matrix and input vectors.
<code>to_dense()</code>	Return the current matrix as a standard (dense) numpy array
<code>transpose()</code>	Return the transpose of the block-sparse matrix

add (A)

Matrix addition of a matrix A to current matrix

Parameters A : matrix

matrix A with same dimensions as current matrix. The matrix A can be an array, *block_sparse* matrix, or *symmetric_block_sparse* matrix. It must have the same block structure as the current matrix if the matrix is a *block_sparse* matrix or *symmetric_block_sparse* matrix.

Returns *block_sparse*

the block-sparse matrix formed by matrix addition of the current matrix to A

dot (A)

Right multiply the current matrix with another *block_sparse* matrix, *symmetric_block_sparse* matrix, or array, A.

Parameters A : matrix

matrix A with compatible dimensions and block structure: i.e. the row blocks of A must match the column blocks of the current matrix, unless A is an array.

Returns *block_sparse*

the block-sparse matrix formed by right multiplication of the current matrix by A

frobenius (A)

Compute the frobenius inner product between the current matrix and matrix A

Parameters A : matrix

matrix A with same dimensions as current matrix. The matrix A can be an array, *block_sparse* matrix, or *symmetric_block_sparse* matrix. It must have the same block structure as the current matrix if the matrix is a *block_sparse* matrix or *symmetric_block_sparse* matrix.

Returns float

the frobenius inner product between the current matrix and matrix A

get_submatrix (*block*)

Retrieve a particular block of the matrix

Parameters *block*: tuple

tuple (i,j) giving the index of the block

Returns block

either an array, a *block_sparse* matrix, or a *symmetric_block_sparse* matrix.

get_type (*block*)

Retrieve the type of a particular block of the matrix

Parameters *block*: tuple

tuple (i,j) giving the index of the block

Returns block type

either array, *block_sparse*, or *symmetric_block_sparse*.

norm ()

Compute the frobenius norm of the current matrix

Returns float

the frobenius norm of the current matrix

qform (*y*, *z=None*)

Computes quadratic form defined by current matrix and input vectors. Let *X* be the current *block_sparse* matrix, and *y* and *z* column vectors. When it is defined, this computes the quadratic form $y'Xz$. If only *y* is provided, this computes the quadratic form $y'Xy$.

Parameters *y*: array

1D numpy array of same length as number of rows of current matrix

z [array] 1D numpy array of same length as number of rows of current matrix. Default None.

Returns float

the value of the quadratic form $y'Xz$

to_dense ()

Return the current matrix as a standard (dense) numpy array

Returns array

transpose ()

Return the transpose of the block-sparse matrix

Returns *block_sparse*

class *block_sparse.symmetric_block_sparse* (*blocks*, *nonzero*, *submatrices*, *dtype=<type 'numpy.float32'>*, *row_names=None*, *col_names=None*)

Define a symmetric block-sparse matrix. Inherits some methods from *block_sparse*.

Parameters *blocks*: array

1D numpy integer array, starting at zero, followed by block boundaries, which are the same for both rows and columns

nonzero : array

symmetric boolean numpy array with number of rows equal to number of row blocks, which is equal to the number of col blocks. If entry [i,j] of nonzero is True, then the corresponding block is non-zero; if it is False, then the corresponding block is zero.

submatrices : list

list of submatrices for non-zero blocks in row-major order, ignoring lower-triangular blocks; e.g., block (1,1), (1,2), (2,2),... Each submatrix can be a array, a *block_sparse* matrix, or a *symmetric_block_sparse* matrix.

dtype : numpy data type object

Set the default data type for the submatrices. Default float32

row_names : array

numpy array with names of the row-blocks. Default None

col_names : array

numpy array with names of the col-blocks. Default None

Returns *symmetric_block_sparse*

block-sparse matrix

Methods

<i>add</i> (A)	Matrix addition of a matrix A to current matrix.
<i>dot</i> (A)	Right multiply the current matrix with another <i>block_sparse</i> matrix, <i>symmetric_block_sparse</i> matrix, or array, A.
<i>frobenius</i> (A)	Compute the frobenius inner product between the current matrix and matrix A
<i>get_submatrix</i> (block)	Retrieve a particular block of the matrix
<i>get_type</i> (block)	Retrieve the type of a particular block of the matrix
<i>norm</i> ()	Compute the frobenius norm of the current matrix
<i>qform</i> (y[, z])	Let X be the current <i>symmetric_block_sparse</i> matrix, and y and z column vectors.
<i>to_dense</i> ()	Return the current matrix as a standard (dense) numpy array
<i>transpose</i> ()	Return the transpose of the symmetric block-sparse matrix

add (A)

Matrix addition of a matrix A to current matrix.

Parameters A : matrix

matrix A with same dimensions as current matrix. The matrix A can be a array, *block_sparse* matrix, or *symmetric_block_sparse* matrix. It must have the same block structure as the current matrix if the matrix is a *block_sparse* matrix or *symmetric_block_sparse* matrix.

Returns matrix

If A is *symmetric_block_sparse*, returns a *symmetric_block_sparse* ma-

trix. Otherwise, returns a *block_sparse* matrix.

get_submatrix (*block*)

Retrieve a particular block of the matrix

Parameters **block** : tuple

tuple (i,j) giving the index of the block

Returns block

either a array, a *block_sparse* matrix, or a *symmetric_block_sparse* matrix.

get_type (*block*)

Retrieve the type of a particular block of the matrix

Parameters **block** : tuple

tuple (i,j) giving the index of the block

Returns block type

either array, *block_sparse* matrix, or *symmetric_block_sparse* matrix.

qform (*y*, *z=None*)

Let X be the current *symmetric_block_sparse* matrix, and y and z column vectors. When it is defined, this computes the quadratic form $y'Xz$. If only y is provided, this computes the quadratic form $y'Xy$.

Parameters **y** : array

1D numpy array of same length as number of rows of current matrix

z [array] 1D numpy array of same length as number of rows of current matrix. Default None.

Returns float

the value of the quadratic form $y'Xz$

to_dense ()

Return the current matrix as a standard (dense) numpy array

Returns array

transpose ()

Return the transpose of the symmetric block-sparse matrix

Returns *symmetric_block_sparse*

the current matrix, as it is symmetric

block_sparse.matmul (*X*, *A*)

Matrix multiplication between *block_sparse* and *symmetric_block_sparse* matrices, as well as matrix multiplication between a *block_sparse* or *symmetric_block_sparse* matrix and an array.

Parameters **X** : matrix

The matrix X can be a *block_sparse* matrix, a *symmetric_block_sparse* matrix, or a array.

A : matrix

The matrix A can be a *block_sparse* matrix, a *symmetric_block_sparse* matrix, or a *array*. Note that the number of rows of A must match the number of columns of X. Furthermore, if X and A are both *block_sparse* or *symmetric_block_sparse*, then the column blocks of X must match the row blocks of A.

Returns *block_sparse*

the block-sparse matrix formed by matrix multiplication XA

`block_sparse.dense_to_block_sparse(dense, blocks, symmetric, dtype=<type 'numpy.float64'>)`

Convert a standard (dense) numpy array into a *block_sparse* or a *symmetric_block_sparse* matrix. Note this simply imposes a block structure onto the matrix so that it can interact with other block matrices. It does not take advantage of any sparsity in the input matrix.

Parameters `dense`: *array*

input matrix

blocks [*list*] list of [row_block_boundaries,col_block_boundaries], where each of row_block_boundaries and col_block_boundaries is a 1D *array* of integers, beginning with 0, followed by the end boundaries of each block in increasing order

symmetric [*bool*] if True, returns a *symmetric_block_sparse* matrix; if False, returns a *block_sparse* matrix

dtype [numpy data type] the default data type of the returned matrix

Returns *matrix*

the current matrix as a *block_sparse* or a *symmetric_block_sparse* matrix

CHAPTER 4

Indices and tables

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